

# Stability of the Accretion Flows with Stalled Shocks in Core-Collapse Supernovae

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*References :* Y&Y, ApJ 650,291 (2006)

Y&Y, ApJ 656,1019 (2007)

# § Introduction

- **Observations** suggest that the explosions are asymmetry (polarization, pulsar kick, images of 1987A).
  - **Multi dimensional simulations** indicate that the accretion flows in SNe are unstable against asymmetric perturbations.
- Hydrodynamical instability is one of the key ingredients of asymmetry (and possibly explosion).

## *Known instability mechanisms :*

convection,

advection-acoustic cycle (Foglizzo 2000, 2001, 2002),

....

# § This study

*We investigated the stability systematically.*

1. First, we found **steady solutions** which mimic the accretion flow with a stalled shock in the core-collapse supernovae, assuming that the neutrino luminosity and the mass accretion rate are constant parameters.
  2. Then the **stability** of the steady solutions was investigated by **global analysis**.
- ★ The **realistic equation of state** by Shen is employed.
  - ★ We took into account both **neutrino heating and cooling**, adopting the realistic reaction rates by Bruenn (1985).

# § Assumptions

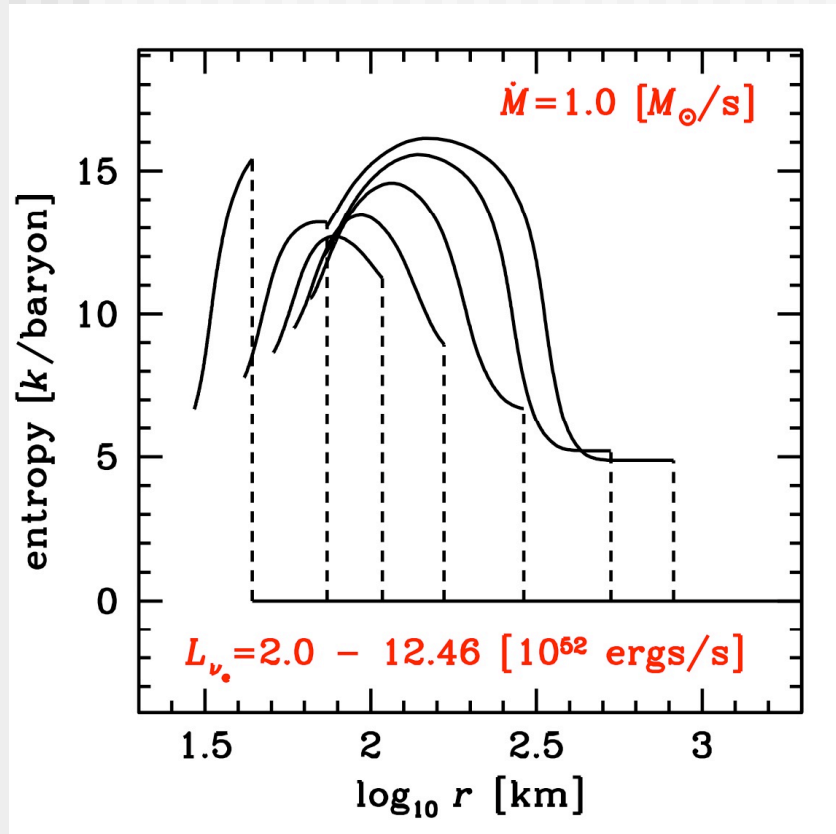
We consider the region between shock and neutrino-sphere.

1. Steady flows are spherically symmetric.
2. Neutrino thin approximation is adopted (i.e., neutrino transfer is not solved).
3. Newtonian gravity is adopted.

## Boundary conditions

- a) Flow outside of the shock is cold free-fall one.
  - b) At the inner boundary (neutrino-sphere), the perturbation of the radial velocity vanishes.
- Perturbations are expanded in the spherical harmonics, and radial dependence of the perturbations are solved globally.

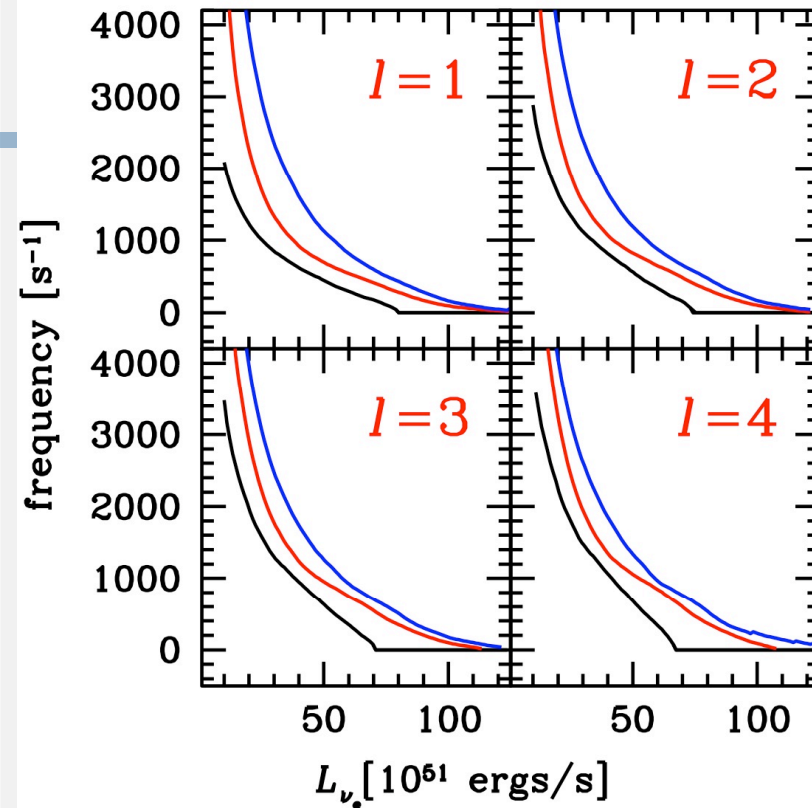
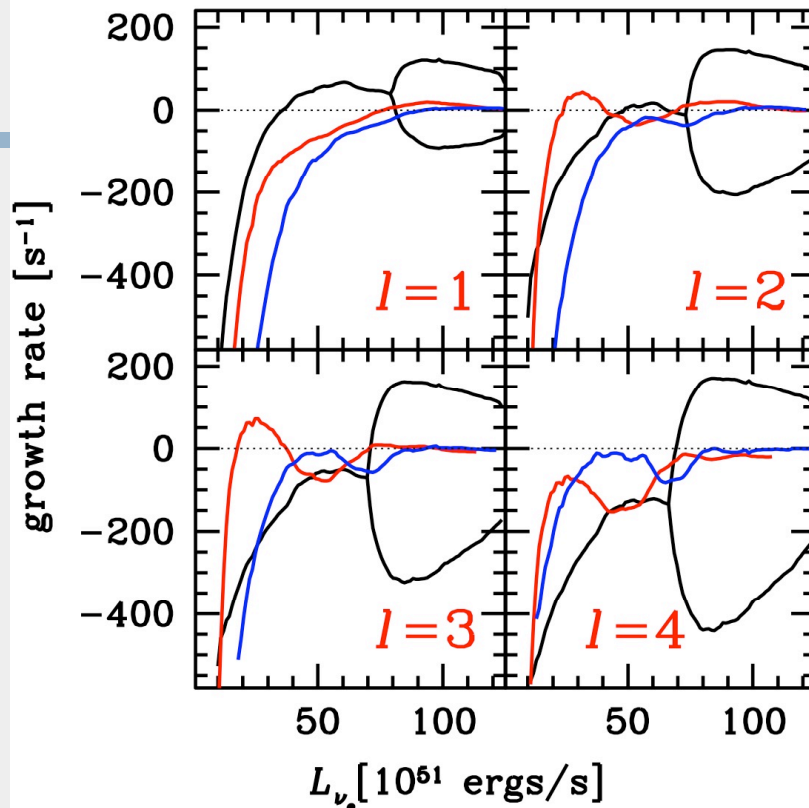
# § Steady solutions



- When the neutrino luminosity exceeds the critical value ( $12.46 \cdot 10^{52} [\text{ergs/s}]$ , for accretion rate  $1.0 [M_{\odot}/s]$ ), there exist **no steady solutions** (Burrows & Goshy 1993).
- When the neutrino luminosity is larger than about  $4.0 \cdot 10^{52} [\text{ergs/s}]$  (for accretion rate  $1.0 [M_{\odot}/s]$ ), there is the **heating layer** where the entropy gradient is negative in the radial direction.

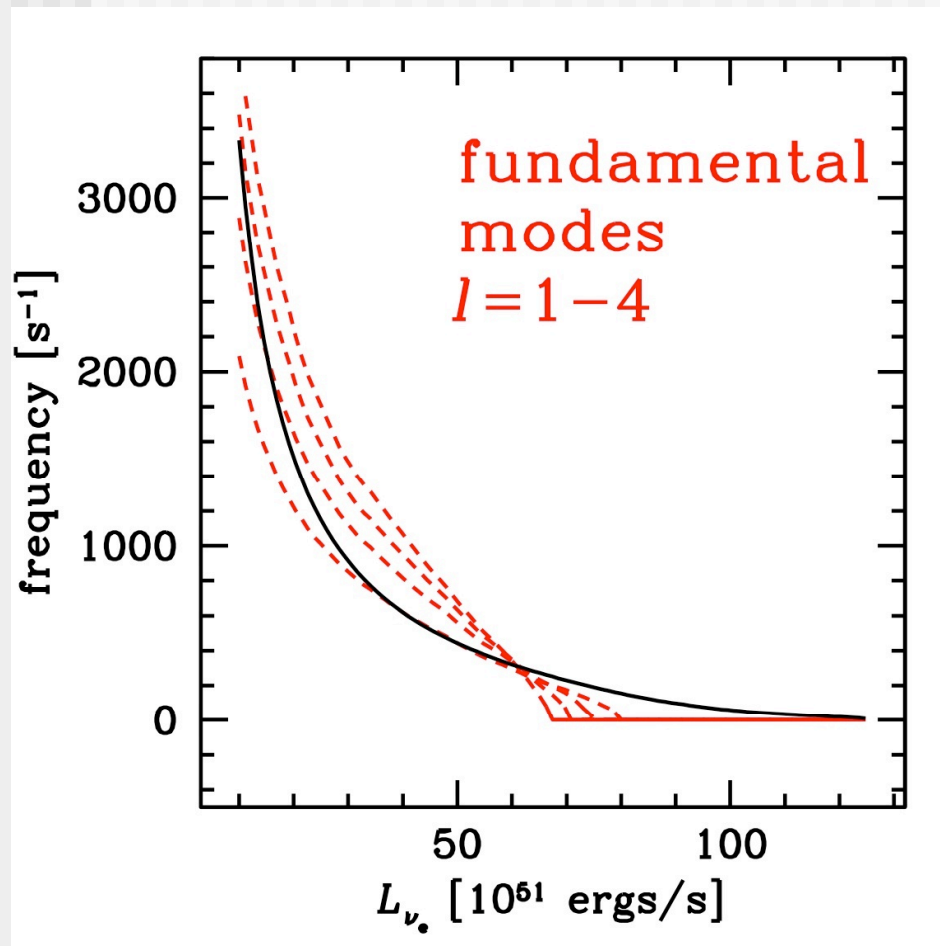
# § Results

## growth rates and frequencies



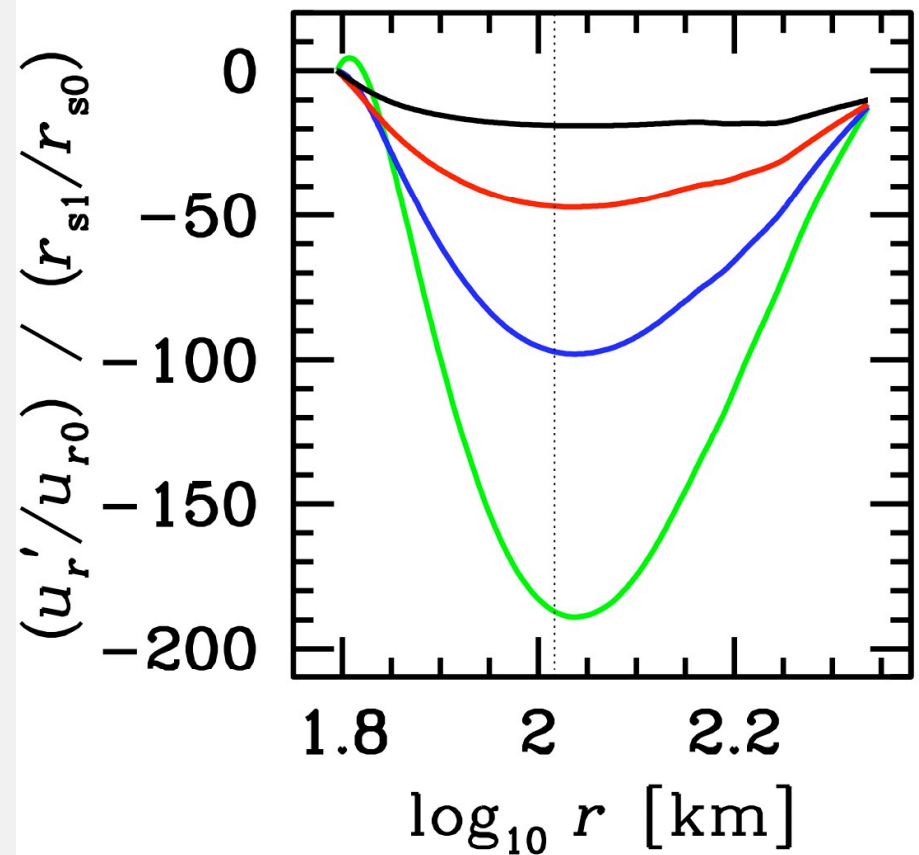
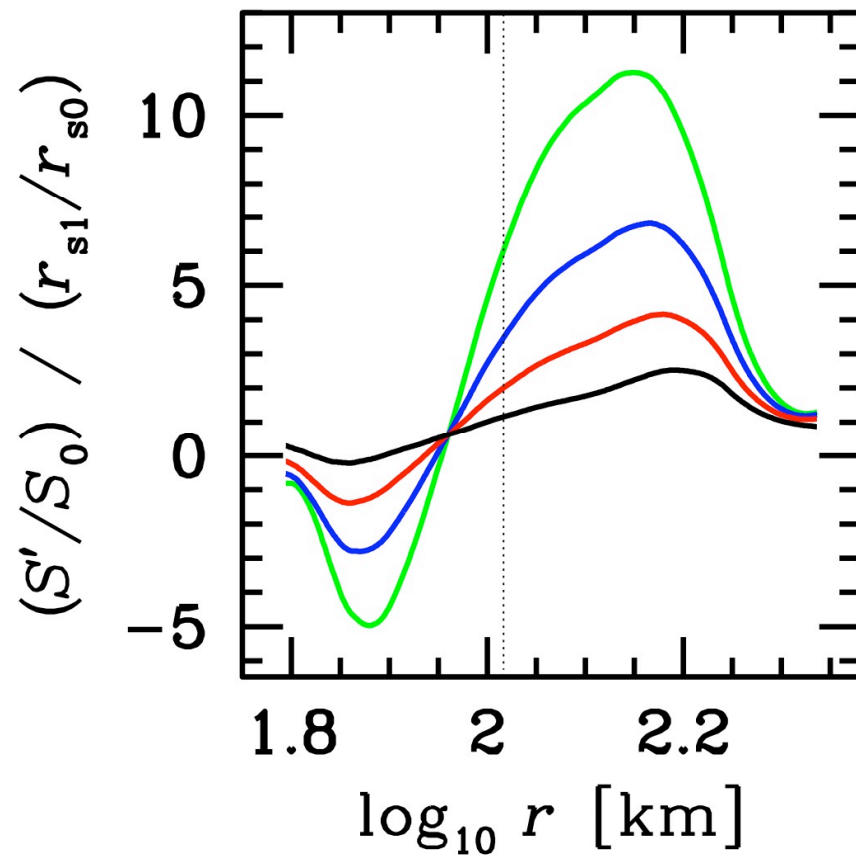
1.  $L_v < 1 \cdot 10^{52} [\text{ergs/s}]$  No unstable mode.
2.  $2 < L_v < 4 \cdot 10^{52} [\text{ergs/s}]$   $l=2,3$  oscillatory modes grow (advection-acoustic).
3.  $3 < L_v < 7 \cdot 10^{52} [\text{ergs/s}]$   $l=1,2$  oscillatory modes grow (advection-acoustic).
4.  $L_v > 7 \cdot 10^{52} [\text{ergs/s}]$  Non-oscillatory modes grow (convection).  
 $l=5-11$  grows fastest (c.f. Foglizzo et al. 2006).

# Frequencies for oscillatory modes



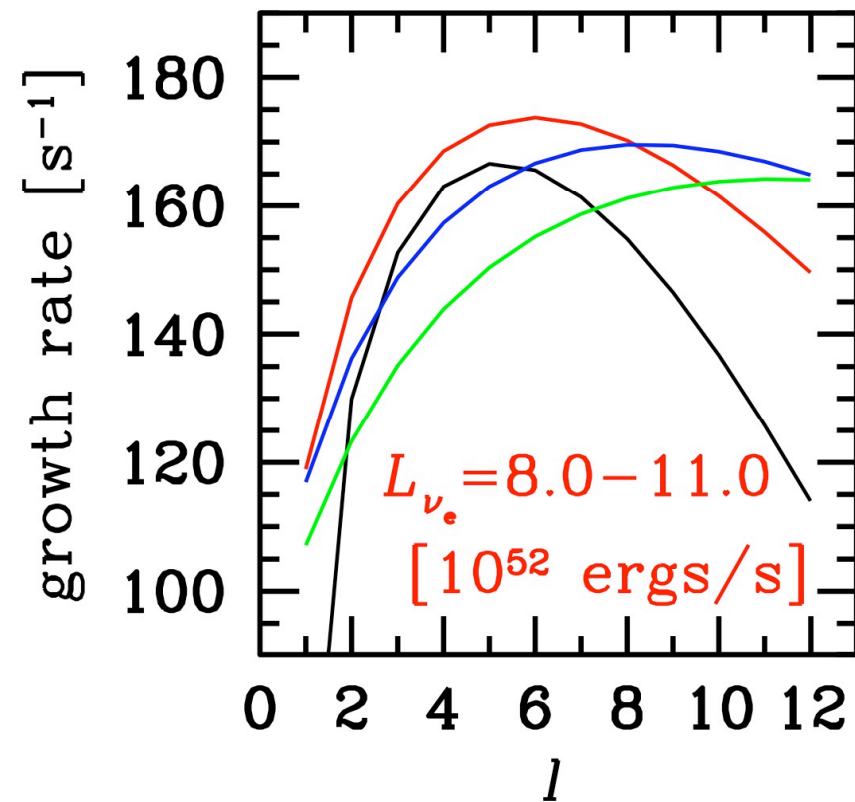
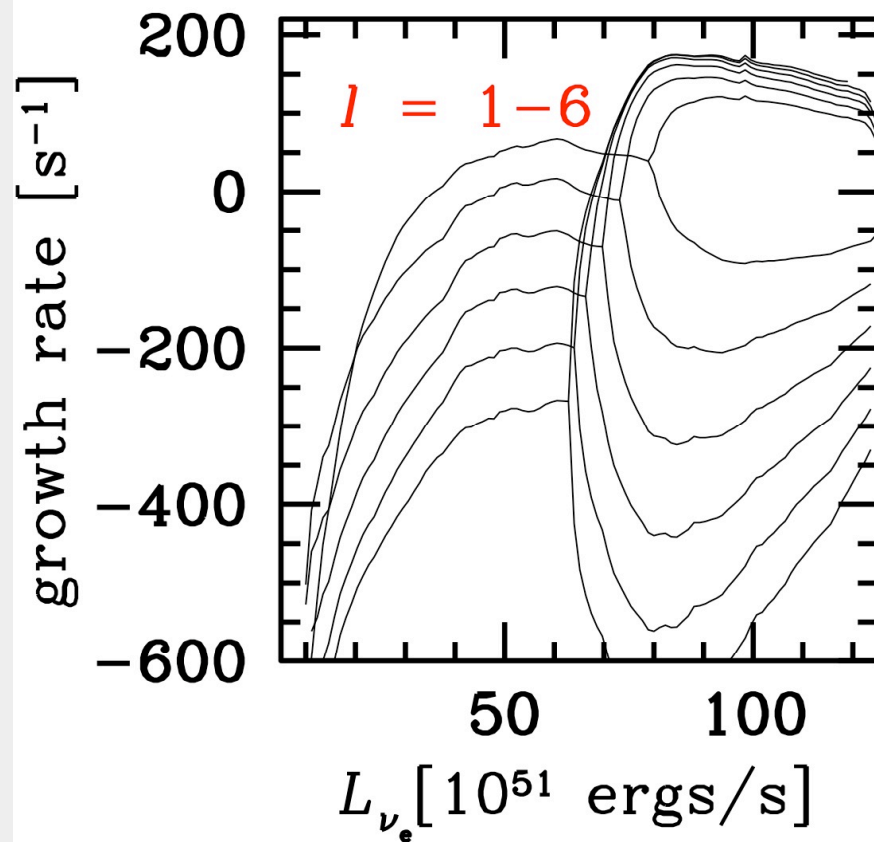
- **Frequencies** are consistent with those predicted by the advection-acoustic cycle.
- **The oscillatory modes** are likely to be the **advection-acoustic cycle** (Foglizzo et al. 2007).
- ★ The stability of the oscillatory modes are affected quantitatively by the inner boundary condition (whereas non-oscillatory modes are not).

# Eigen-functions of non-oscillatory modes





# Growth rates for convective modes



# § Summary

For mass accretion rate  $1.0 [M_{\odot}/s]$ ,

- 1)  $L_v > 12.46 \cdot 10^{52} [\text{ergs/s}]$  No steady solutions.
- 2)  $L_v > 4 \cdot 10^{52} [\text{ergs/s}]$  Heating region emerges.
  
1.  $L_v < 1 \cdot 10^{52} [\text{ergs/s}]$  No unstable mode.
2.  $2 < L_v < 4 \cdot 10^{52} [\text{ergs/s}]$   $l=2,3$  advection-acoustic modes grow.
3.  $3 < L_v < 7 \cdot 10^{52} [\text{ergs/s}]$   $l=1,2$  advection-acoustic modes grow.
4.  $L_v > 7 \cdot 10^{52} [\text{ergs/s}]$  Convective modes grow ( $l=5-11$  grow fastest).
  
- ★ Even when the radial gradient of entropy is negative, the convection does not always take place because of the advection (Foglizzo et al. '06).
- ★ The advection-acoustic cycle and the convection become important in different aspects.